

THE IDEAL GAS LAW

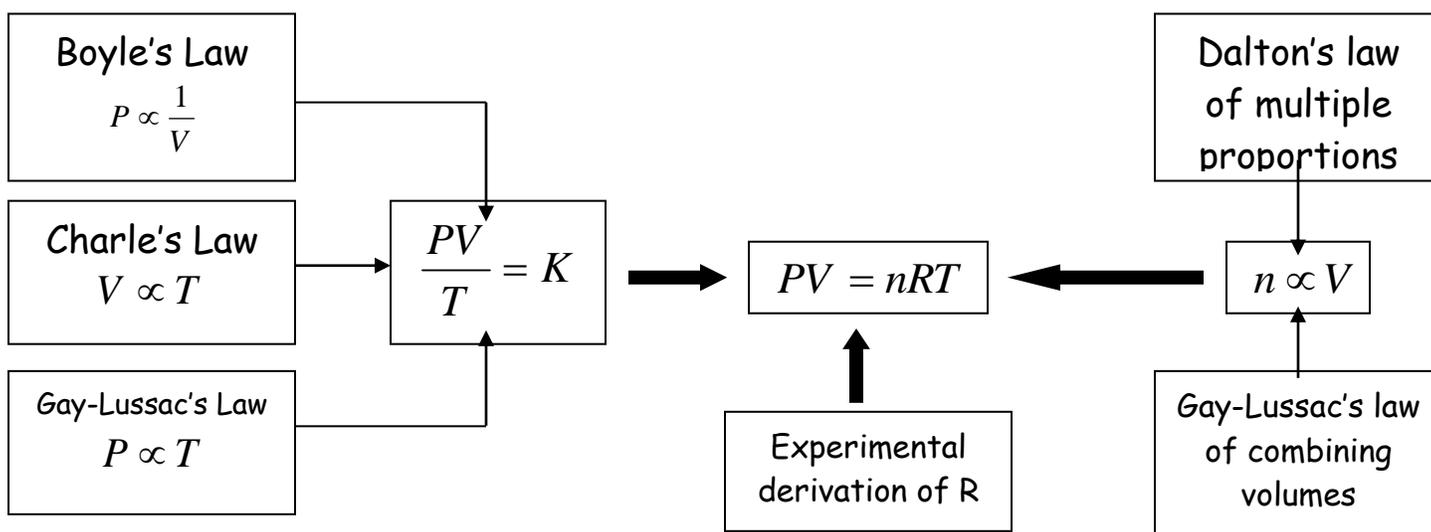
- Recall that the molar volume of an “ideal gas” is 22.4 L at STP conditions
- An ideal gas is a **hypothetical** gas that obeys the gas laws perfectly under ALL conditions. i.e. won't condense into a liquid when cooled, graphs are all perfectly straight lines, etc.
- According to the KMT of an ideal gas;
 - gas molecules have insignificant volume
 - there are no attractive forces between molecules
 - molecules move in perfectly straight lines
 - collisions are completely elastic (do not lose energy)

At STP most gases do behave like ideal gases, however, at high pressures and/or low temperatures, most gases no longer behave ideally.

Scientists that desire more accuracy in their experiments have adopted the **Ideal Gas Law** to reflect the behavior of real gases.

The **Ideal Gas Law** is a mathematical representation of the relationship between moles, pressure, volume, and temperature for an ideal gas.

CONCEPT ORGANIZER: The Evolution of the Ideal Gas law



- Ideal Gas Law is derived by combining the **Boyles' law**, **Charles's law** and **Avogadro's Law/Hypothesis**.

$$V \propto n \quad \text{and} \quad V \propto \frac{T}{P} \quad \text{combined becomes,} \quad V \propto \frac{nT}{P}$$

- Introducing a constant, k_4 the formula becomes, $k_4 = \frac{PV}{nT}$, *but what is k_4 ?*
- To find the value of R, we would substitute known values and solve for R.
Example: At STP (101.3 kPa and 273.15K), 1.00 mol of an ideal gas would occupy a volume of 22.4L.

$$PV=nRT \quad R=\frac{PV}{nT} \quad R = \frac{101.325\text{kPa} \times 22.414\text{L}}{1.00\text{mol} \times 273.15\text{K}} = \underline{\underline{\mathbf{8.314 \text{ kPa}\cdot\text{L}}}} \underline{\underline{\mathbf{\text{mol}\cdot\text{K}}}}$$

- If the mass of gas was given, and not moles, we would have to calculate n first.
- The accurate value of $8.314 \frac{\text{kPa}\cdot\text{L}}{\text{mol}\cdot\text{K}}$, determined experimentally, is known as the **universal gas constant**, and is given the symbol **R**.

$$\text{OR} = 0.08206 \text{ L}\cdot\text{atm}/\text{mol}\cdot\text{K} \text{ (see next page)}$$

- Rearranging the formula to the usual form of the **IDEAL GAS LAW**:

$$PV = nRT$$

Recall, any gas that obeys this equation is called an "ideal gas".

NOTE: there is no such thing as an ideal gas, however at low pressures (~1 atm) and room temperature conditions, gases will behave like an ideal gas and obey $PV=nRT$

Guidelines for using the Ideal Gas Law

- Always convert the temperature to Kelvins (K).
- Always convert the masses to moles (mol).
- Always convert the volumes to litres (L).
- Using the ideal gas law will always be easier if pressure values are converted to kilopascals (kPa). Then the value of R that is required will always be $8.314 \frac{\text{kPa}\cdot\text{L}}{\text{mol}\cdot\text{K}}$. *What can you do if you forget this value?*

Converting the units of the Universal Gas Constant, R

Rather than converting pressure to kilopascals, we can convert the units of R .
If pressure is given in atmospheres, atm:

$$\frac{8.314 \cancel{\text{kPa}} \cdot \text{L}}{\text{mol} \cdot \text{K}} \times \frac{1 \text{ atm}}{101.3 \cancel{\text{kPa}}} = 0.08206 \frac{\text{atm} \cdot \text{L}}{\text{mol} \cdot \text{K}}$$

If pressure is given in torr (or mm Hg):

$$\frac{8.314 \cancel{\text{kPa}} \cdot \text{L}}{\text{mol} \cdot \text{K}} \times \frac{760 \text{ mmHg}}{101.3 \cancel{\text{kPa}}} = 62.37 \frac{\text{mmHg} \cdot \text{L}}{\text{mol} \cdot \text{K}}$$

Sample Problem

If 0.78g of hydrogen at 22°C and 125kPa is produced, what volume of hydrogen would be expected?

Given: mass of H₂ = 0.78g T = 22 °C P = 125 kPa R = 8.314 $\frac{\text{kPa} \cdot \text{L}}{\text{mol} \cdot \text{K}}$
V = ?

Plan: Step 1: Find moles of hydrogen
Step 2: Use the Ideal Gas Law to find the volume of hydrogen expected.

Solution: Step 1: $n = m/M = 0.78\text{g}/2.02\text{g/mol} = 0.39\text{mol}$
Step 2: $PV = nRT$
 $V_{\text{H}_2} = \frac{nRT}{P}$
 $V_{\text{H}_2} = \frac{0.39\text{mol} \times 8.31\text{kPa} \cdot \text{L/mol} \cdot \text{K} \times 295\text{K}}{125\text{kPa}}$
 $V_{\text{H}_2} = 7.6\text{L}$

Paraphrase: Therefore the volume of hydrogen gas expected was 7.6L.

Practice Problem

What mass of neon gas should be introduced into an evacuated 0.88L tube to produce a pressure of 90. kPa at 30°C? (A: 0.56 g Ne)